## **Subject: Physics**

## Paper: VII

## (Old Syllabus)

Time: 2 Hours

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

Answer any TEN questions from the following:

1. Show that

$$\int_{-\infty}^{+\infty} \frac{x^2 dx}{(x^2+1)^2 (x^2+2x+2)} = \frac{7\pi}{50}$$

## 2. Evaluate

(i) 
$$\oint_c \frac{\sin 3z}{z + \frac{\pi}{2}} dz$$
, if *c* is the circle  $|z| = 5$   
(ii)  $\oint_c \frac{e^{iz}}{z^3} dz$ , if *c* is the circle  $|z| = 2$ 

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3. State the Hamilton's variational principle. Use this principle to find the equation of motion of a simple pendulum.

4. What are generalized co-ordinates? Obtain an expression for the generalized force and generalized potential.

5. Consider a system of particles obeying Maxwell Boltzmann statistics and the energy of each particle can be expressed as  $E(x) = ax^2$ ,  $-\infty \le x \le \infty$ . Find the average energy per particle of the system. Relate it to the principle of equipartition of energy. 5

P. T. O.

 $5 \times 10 = 50$ 

Full Marks: 50

5

6.	Consider an electron gas in a metal at $T = 0$ K. Calculate the mean energy of an electron	n
in term	s of the Fermi energy of the metal.	5
7.	Derive Einstein's equation for the Brownian motion.	5

8. Using Langevin's theory, show that at high temperature and small electric field, orientational polarization is inversely proportional to the absolute temperature. 5

9. describe an experiment with suitable diagram to measure the Hall coefficient and Hall voltage.5

10. Adopting the free electron theory of metals, find out an expression of the electrical conductivity. 5

11. Derive Laue equations of diffraction of X-rays and obtain Bragg's law from them. 5

12. Using quantum theory of paramagnetism, derive an expression for the paramagnetic susceptibility at high temperature and low magnetic field.